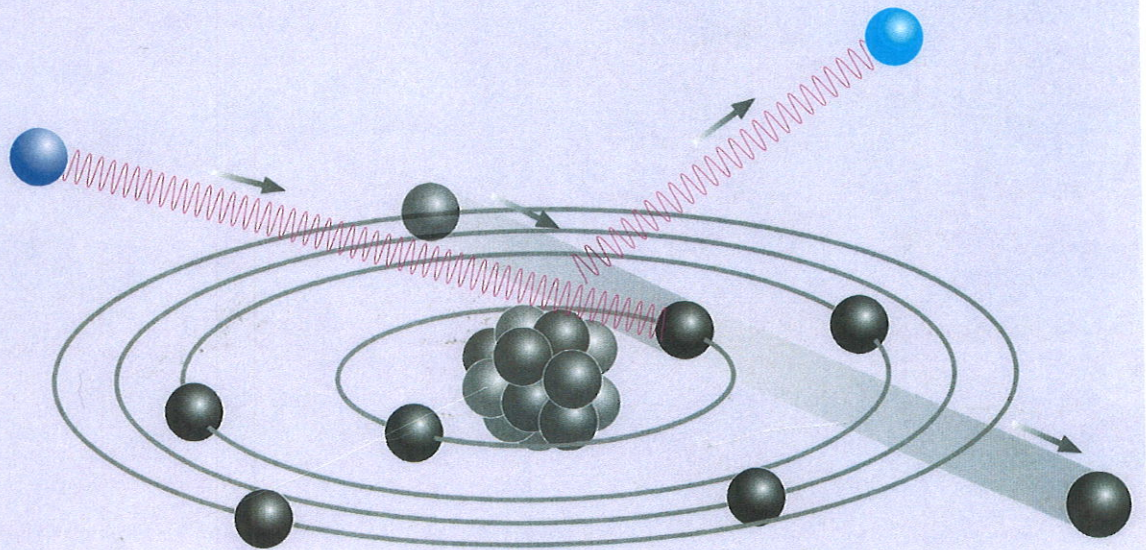


# *Understanding* **XRF** *Spectrometry*

A practical guide  
with worked  
examples

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## Volume

Basic concepts  
and  
instrumentation

# 1

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